



CENTRO DE  
**MATEMÁTICA**  
UNIVERSIDADE DO PORTO

GEOMETRY AND TOPOLOGY SEMINAR

# The moduli space of Higgs bundles over a real curve and the real Abel-Jacobi map

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**Abstract.** The moduli space  $M_C$  of Higgs bundles over a complex curve  $X$  admits a hyperkaehler metric: a Riemannian metric which is Kaehler with respect to three different complex structures  $I, J, K$ , satisfying the quaternionic relations. If  $X$  admits an anti-holomorphic involution, then there is an induced involution on  $M_C$  which is anti-holomorphic with respect to  $I$  and  $J$ , and holomorphic with respect to  $K$ . The fixed point set of this involution,  $M_R$ , is therefore a real Lagrangian submanifold with respect to  $I$  and  $J$ , and complex symplectic with respect to  $K$ , making it a so called *AAB*-brane. In this talk, I will explain how to compute the mod 2 Betti numbers of  $M_R$  using Morse theory. A key role in this calculation is played by the Abel-Jacobi map from symmetric products of  $X$  to the Jacobian of  $X$ .

FRIDAY, JUNE 02

11:30

ROOM 1.09

Please note the unusual time

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